Bulk-phase viscoelastic properties of seawater

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ABSTRACT

Deformation and mixing in any medium are controlled by its viscosity and elasticity. The present study provides preliminary information, at oceanic shear rates, on the viscosity and elasticity in the bulk phase of seawater.

Thirty-two samples of seawater, obtained on cruises at four times of year in a meso-oligotrophic part of the Mediterranean, were measured for bulk-phase viscoelastic properties in an oscillating-shear Couette flow with measuring gap 0.5 mm, over shear rates $\dot{\gamma}$ from 0.0021 to 0.286 s$^{-1}$. Fifteen samples were obtained on a single cruise in the German Bight, North Sea, when Phaeocystis blooms were taking place, and these were similarly measured at $\dot{\gamma}$ from 0.0021 to 0.973 s$^{-1}$.

The bulk-phase measurements suffered interference contributed by the surface film. The interference mechanism was investigated, and a method was developed to correct for it, which permitted extraction of the bulk-phase viscosity. While extraction of bulk-phase elastic effects was possible only in the most thickened Mediterranean samples, in the generally thicker North Sea samples bulk-phase elasticity was closely related to bulk-phase excess (polymeric) viscosity.

\[ \eta_0^{\gamma} \]

At $\dot{\gamma} = 0.0021$ s$^{-1}$, viscosity, $\eta_0$, in the Mediterranean samples ranged from 0.1 to 19 (mean 3.5, n = 23) times the average solution viscosity, $\eta_{so}$, which is $\gamma$-independent and contributed principally by water and salt. Corresponding values for the German Bight samples were 0.99 to 127 (mean 52, n = 5) times $\eta_{so}$.

For each cruise, the overall excess viscosity, $\eta_E = \eta_0 - \eta_{so}$, showed a power-law relationship with $\dot{\gamma}$ such that $\eta_E = k \dot{\gamma}^2$. For the five different cruises, $P$ varied from 1.1 to 1.5. Such high values of $P$ indicate that thickening is contributed principally by cross-linked polymer gel rather than by overlapping chains. The elastic modulus $G'$ was very variable, with sample maxima of 100 and 300 μPa in the Mediterranean and North Seas respectively.

Thickening (determined as both $\eta_E$ and $G'$) was heterogeneous, with a variability coefficient (SD/mean) from 1 to 3 for different cruises and values of $\dot{\gamma}$. In the three Mediterranean cruises in which duplicate measurements were made for the same samples, all the variability could be accounted for by in-sample variability, suggesting that centimetre-scale flocculation-type processes were responsible. Gaussian
standard deviation $SD_G$ was constant (indicating self-similarity) for the higher values of $\eta_E$ both the Mediterranean and North Sea studies as well as for $G'$ in the North Sea study. At the lower end of the $\eta_E$ and $G'$ distributions, $SD_G$ was higher, due to experimental variability. Over a range of appropriate shear rates, the turbulent (Kolmogorov) length scale $L$ was calculated using the mean viscosities measured. The calculations suggest that, when turbulence is low or biological activity high, $L$ is considerably higher than values previously supposed, and mixing correspondingly reduced. The heterogeneous nature of both $\eta_E$ and $G'$ must furthermore increase intermittence in both turbulence and mixing. It is concluded that a significant part of the sea functions as a lumpy, biopolymeric gel in which small-scale ($\lesssim 100\,L$) flow and mixing are under strong biological influence.


RÉSUMÉ

Propriétés viscoélastiques de la phase volumique d’eau de mer

La déformation et le mélange de tout milieu sont contrôlés par sa viscosité et son élasticité. L’étude présente fournit des informations préliminaires, à des vitesses de déformation ambiantes en mer, sur la viscosité et l’élasticité en phase volumique (c’est-à-dire celle de masse) de l’eau de mer.

Trente-deux échantillons d’eau de mer ont été prélevés pendant quatre sorties réparties sur toute une année dans une zone méso-oligotrophe de la Méditerranée. Des mesures des propriétés viscoélastiques de la phase volumique ont été effectuées sur ces échantillons en régime d’écoulement oscillant entre deux cylindres coaxiaux, avec un entrelacement de 0,5 mm et sur une gamme de vitesses de cisaillement $\dot{\gamma}$ entre 0,0021 et 0,286 s$^{-1}$. Quinze échantillons ont été prélevés également en baie d’Helgoland (Mer du Nord) durant des efflorescences de Phaeocystis, puis ils ont été mesurés de manière identique à des valeurs de $\dot{\gamma}$ entre 0,0021 et 0,973 s$^{-1}$.

Les mesures effectuées sur la phase en volume ont été parasitées par des effets aménés par la phase superficielle. Le mécanisme responsable de ces effets parasites a été étudié et une méthode pour en tenir compte a été développée. A cause de ces parasites les effets élastiques de la phase volumique n’ont pas pu être décelés dans la plupart des échantillons méditerranéens, mais dans l’eau de la Mer du Nord l’élasticité était étroitement liée à la viscosité excédentaire (due aux polymères).

Pour $\dot{\gamma} = 0,0021 \, s^{-1}$, la viscosité, $\eta$, mesurée sur les échantillons de la Méditerranée, a varié entre 0,0072 et 0,019 ( moyenne 3,5; n = 23) fois la «viscosité du solvant», $\eta_w$ qui est indépendante de $\dot{\gamma}$ et qui provient principalement de l’eau et du sel. Les valeurs correspondantes pour la baie d’Helgoland ont été 0,99 à 127 (moyen 52, n = 5) fois $\eta_w$.

La viscosité excédentaire, $\eta_E = \eta - \eta_w$, obéit à une loi en puissance : $\eta_E = k \cdot \dot{\gamma}^{P}$. Pour chacune des cinq sorties en mer, la valeur globale de $P$ s’est située entre 1,1 et 1,5. Ces valeurs importantes de $P$ démontrent que l’épaississement est produit par des gels de polymères portant de nombreuses zones de jonction. Le module élastique $G'$ a été très variable, avec un maximum de 100 ou de 300 μPa, respectivement pour l’étude en Méditerranée ou celle en Mer du Nord.

Ces épaississements ($\eta_E$ et $G'$) étaient hétérogènes, le coefficient de variabilité (écart-type/moyenne) étant de 1 à 3, à une valeur donnée de $\dot{\gamma}$, pour chacune des sorties. Pour les trois sorties en Méditerranée où des mesures en double ont été effectuées sur les mêmes échantillons, toute la variabilité aurait pu être due à des effets à l’intérieur des échantillons. Des processus flucatifs à l’échelle centimétrique auraient pu être responsables de cette hétérogénéité. L’écart-type gaussien $SD_G$ est constant pour les valeurs les plus élevées de $\eta_E$ ou de $G'$, où il représente la variabilité (auto-similaire) du milieu. Dans la partie la plus basse, $SD_G$ devient plus élevé, dû probablement à des imprécisions de mesure.

Sur la gamme de $\dot{\gamma}$ ambiante en mer, l’échelle de longueur de turbulence (de Kolmogorov) $L$ a été calculée à partir des viscosités moyennes mesurées. Ces cal-
INTRODUCTION

Old measurements of seawater viscosity (Krümmel, 1907; Miyake and Koizumi, 1948) made at shear rates two to seven orders of magnitude higher than general ambient values (Jenkinson, 1990) are still used in modelling turbulence and calculating energy dissipation in the sea. The Navier-Stokes equations and Kolmogorov’s (1941 a; b) model of turbulence, to which current models of marine turbulence refer, assume the medium to be Newtonian, that is without elasticity and with viscosity independent of shear rate. It has been suggested, however, that easily seen mucus sheaths as well as more dispersed polymers excreted by algae represent increased “structural viscosity”, and are used by phytoplankton to manage flow fields (Margalef, 1957; 1978; Hutchison, 1967; Sournia, 1982; Jenkinson and Wyatt, 1992; Jenkinson, 1993). Moreover adsorption kinetics in natural waters suggest that some filter-passing colloids function as surfaces (Morel and Gschwend, 1987), and must therefore be functionally solid in situ. The way ambient viscosity and elasticity vary thus has to be known in order to understand biomodification of flow, dispersion, particle sinking, aggregation/disaggregation (Jenkinson, 1986; Jenkinson et al., 1991; Fogg, 1991), solute dynamics (Morel and Gschwend, 1987) and wave propagation (Saasen and Hassager, 1991).

Offshore, photic-zone concentrations of around 3 g C m⁻³ of dissolved (including most of the colloidal) organic matter (DOM) appear general, of which about 20 % still exceed 100 kdaltons in molecular weight after passing through an injector (Sugimura and Suzuki, 1988). In an imaginary sea devoid of gravitation and flow, aggregates would flocculate out from the dissolved and particulate organic matter (respectively DOM and POM) and continue to grow roughly fractally and indefinitely (Benoit, 1984, cited by Prost and Rondelez, 1991). Even in the real sea, aggregated mucus “clouds” have been seen filling the whole volume between depths of 4 and 9 m over hundreds of square kilometres in the eutrophic northern Adriatic (Stachowitsch et al., 1990). That such networks are able to resist break-up in the tidal waters of the northern Adriatic and that one-metre aggregates roll along the sea bed during current flow (Stachowitsch et al., 1990), with its associated shearing, shows that they impart to the water not only increased viscosity, but also a yield stress (the stress below which the material does not flow, Barnes et al., 1989) at length scales similar to the aggregate dimensions. That bubbles visible to the naked eye are trapped in exceptional algal blooms and in aggregates indicates a yield stress of at least 0.2 Pa (Jenkinson, 1990), while the ability of birds to land on some, perhaps dried, floating aggregates (Stachowitsch et al., 1990) indicates a cm- to dm-scale yield stress of ≥ 100 Pa. The negative relationship between excess viscosity and shear rate, found in phytoplankton cultures, suggested to Jenkinson (1986) that the highest values of viscosity at ambient shear rates in the sea might as probably be associated with low-shear deep-ocean water as with higher-shear, near-surface, productive zones rich in DOM.

The objective of the present study was to repeat the old measurements of viscosity in bulk seawater, but at shear rates within the ambient oceanic range, and to measure elasticity at the same time. First, the top 100 m of meso-oligotrophic Mediterranean water was investigated at a single station at four times of year. Shear forces were measured in a rheometer at shear rates from 0.0021 to 0.286 s⁻¹. For comparison, similar measurements were made at shear rates from 0.0021 to 0.973 s⁻¹ on sea water taken from a single cruise in shallow waters of the German Bight during patchy plankton blooms. Existing rheometrical and statistical methods were adapted to increase detection limits. In order to correct for mechanical interference of bulk-phase measurements by the surface film, the rheological nature of this surface-film interference was also investigated.

METHODS

Mediterranean study area, sampling and sample handling

Mediterranean samples were obtained at or near a single station about 1 km off the coast in a water depth of 200 m (latitude 43°41’N, longitude 7°21’E) in the rade de Villefranche, France. Appendix Table 1 gives details. Surface slicks and boat wakes were avoided.

Samples of 1 dm³ were obtained using Van Doorn bottles and immediately transferred to storage bottles through a 0.45 mm mesh. This treatment subjected the water to a shear rate estimated at 10⁶ to 3 x 10⁷ s⁻¹ for several tenths of a second. Within twenty minutes of sampling, the samples were packed in ice, then taken to Grenoble, and their rheology investigated in a temperature-controlled laboratory. Two to four hours before beginning the measurement of each sample, its storage bottle was mixed by gentle inversion, and a subsample of 20 cm³ poured into a test tube to warm in a water bath set to laboratory temperature. Measurements were made 20 to 48 h after sampling.
Appendix Table 1
Oceanographic data for each Mediterranean cruise.

<table>
<thead>
<tr>
<th>Date</th>
<th>Time (GMT)</th>
<th>Depth sampled (m)</th>
<th>Salinity in situ</th>
<th>Temperature in situ</th>
<th>Density stratification</th>
<th>Temperature of measurement (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8 Jul 1986</td>
<td>1230</td>
<td>0°, 0°, 2°</td>
<td>37.9-38.3°</td>
<td>24.0-14.0°</td>
<td>2.9°</td>
<td>25 ± 0.5</td>
</tr>
<tr>
<td>18 Nov 1986</td>
<td>1650</td>
<td>0°, 2°, 10, 20°</td>
<td></td>
<td>17.5-17.1°</td>
<td>0.15°</td>
<td>21 ± 1</td>
</tr>
<tr>
<td>11 Mar 1987</td>
<td>1320</td>
<td>0°, 2°, 10, 25°</td>
<td></td>
<td>12.8-12.9°</td>
<td>0.002°</td>
<td>22 ± 1</td>
</tr>
<tr>
<td>21 May 1987</td>
<td>0900</td>
<td>0°, 2°, 10, 25°</td>
<td></td>
<td>20-14°</td>
<td>1.5°</td>
<td>22 ± 1</td>
</tr>
</tbody>
</table>

* - collected at surface 2 m from Villefranche Zoological Station Jetty; ** - not strained; X - sampled by bucket; - = for depths 0-75 m. ♦ - based on data for previous years; ♦ - from records of Villefranche Zoological station; □ - derived, using tables (Unesco, 1961), from temperature and salinity. Surface slicks and boat wakes were avoided. Phytoplankton levels were never high (yellow sampling bottle always visible from boat at 210 m).

North Sea study area, sampling and sample handling

North Sea samples were obtained on 8 June 1988 at three stations near Helgoland, in depths of water from 15 to 45 m. Stations were selected in which a surface-mixed layer, a principal pycnocline and a bottom-mixed layer were all fairly well defined. Samples were taken by Niskin bottle in these three layers, from the sea-surface microlayer using a glass plate (Harvey and Burzell, 1972), and from the benthic microlayer of amorphous "fluff" using a Reineck box corer. Further details will be given by Jenkinson and Biddanda (in preparation).

Rheometry: theoretical considerations

In sinusoidal deformation (that imposed in *Sinus* mode), the shear rate, \( \dot{\gamma} \) varies 90° ahead of the shear \( \gamma \). In a perfectly elastic solid with negligible viscosity, the shear stress, \( \tau \), then varies in phase with the imposed \( \gamma \). For a Newtonian liquid, by contrast, \( \tau \) varies 90° ahead of \( \gamma \) (i.e., stress and strain are 90° out of phase). For real materials, the elastic and viscous components of resistance to deformation may be separated by resolving the resultant stress into its in-phase and out-of-phase components. The ratio of in-phase stress to applied strain is the elastic modulus, \( G' \), while the corresponding parameter for the out-of-phase response is the viscous modulus, \( G'' \). The energy used in deforming an elastic solid is stored, and then recovered as the sample springs back to its original shape. For a perfect liquid, however, there is no such recovery, and all the energy used in deformation is lost (as heat). Hence \( G' \) and \( G'' \) are also known as the "storage" and "loss" moduli, respectively. The overall response of the sample may be characterized by the complex shear modulus,

\[
G^* = [(G')^2 + (G'')^2]^{0.5}
\]

(1)

The viscosity,

\[
\eta = G''/\dot{\gamma}
\]

(2)

The viscosity in some phytoplankton cultures was considered by Jenkinson (1986) to consist of two components such that

\[
\eta /\dot{\gamma} = \eta_W + \eta_E /\dot{\gamma}
\]

(3)

where \( \eta_W \), the viscosity of the aquatic phase, equivalent to the "solvent viscosity" in polymer solutions (Morris, 1984), was independent of \( \dot{\gamma} \), while over ± wide ranges of \( \dot{\gamma} \) the excess viscosity followed the Ostwald power-law model (Morris, 1984):

\[
\eta_E /\dot{\gamma} = k /\dot{\gamma}^P
\]

(4)

where \( k \) and \( P \) remain constant. Rheological characterisation was carried out using a *Low Shear 30* rheometer (Contraves AG, Zürich) at the Centre de Recherches sur les Macromolécules Végétales (Centre National de la Recherche Scientifique), the "Grenoble rheometer", and a second rheometer of the same model at the Alfred-Wegener-Institut, Bremerhaven, the "Bremerhaven rheometer".

Figure 1

Cross sections of three Couette systems (CS): a) the short CS; b) the tall CS; c) the "surface" CS; d) schematic CS to show dimensions mentioned in Table 1.

Section verticale des trois Systèmes Couette (SC) utilisés: a) le petit SC; b) le grand SC; c) le SC pour mesurer la théorie de la couche superficielle; d) schéma d'une SC pour montrer les dimensions données dans le tableau 1.
Table 1

<table>
<thead>
<tr>
<th>Dimension (mm)</th>
<th>Tall CS</th>
<th>Short CS</th>
<th>Surface film CS</th>
</tr>
</thead>
<tbody>
<tr>
<td>L</td>
<td>20.0</td>
<td>8.0</td>
<td>0.0</td>
</tr>
<tr>
<td>r₁</td>
<td>5.5</td>
<td>5.5</td>
<td>3.0</td>
</tr>
<tr>
<td>r₂</td>
<td>6.0</td>
<td>6.0</td>
<td>6.0</td>
</tr>
<tr>
<td>r₃ Surf</td>
<td>12.21</td>
<td>9.37 to 12.6</td>
<td>6.0</td>
</tr>
<tr>
<td>r₃ stem</td>
<td>1.0</td>
<td>1.0</td>
<td>n/a</td>
</tr>
</tbody>
</table>

M'fctur'-s. spc 2T-2T 1-1 1-6

L: height of bob; r₁: radius of bob; r₂: radius of cup in region of bulk-phase measurement; r₃ Surf: radius of cup in region of surface film; r₃ Stem: radius of bob stem; n/a: not applicable.

The sample to be measured was placed in a cylindrical cup, and a bob, suspended coaxially with the cup, was lowered slowly into the test material. This geometry of coaxial cylinders is known as a Couette system (CS). Two geometries of CS were employed, a “tall CS” (Fig. 1 a) and a “short CS” (Fig. 1 b). To investigate surface effects, a surface bob was used as shown in Figure 1 c. Table 1 gives the dimensions of these systems (Fig. 1 d).

A sample is sheared by rotating the cup of the CS at a known angular velocity. A shearing force is transmitted across the test sample in the measuring gap (Fig. 1 a, b), where it exerts a tangential force on the vertical surface of the bob. This is translated into a torque tending to turn the bob. The instrument reacts to keep the bob from turning by causing an electric current to flow in a coil such that it generates an equal and opposite torque. For a given CS geometry, this current is thus proportional to the torque and hence to the total shear stress, \( \tau \). Smaller forces generated by shearing in the bulk material situated between the bottom of the bob and that of the cup, as well as in the upper part of the CS between the bob stem and the upper wall of the cup, are allowed for in the manufacturers’ calibration coefficients. The surface film lying between the upper wall of the cup and the bob stem may also transmit tangential forces to the bob stem, and hence torque to the bob. Although surface-film effects are generally neglected in CS measurements, the bulk-phase rheological structure in seawater is much weaker than that generally measured by rheologists. As will be shown, the torque due to surface-film effects therefore interfered with measurements of rheological properties in the bulk liquid, and had to be corrected for.

The rheometers could be operated in two modes, Rotational and Sinus. In Rotational mode, the angular velocity of the cup, and hence the shear rate of the test material, \( \dot{\gamma} \), could be controlled step-wise, but the cup could be rotated only clockwise. In Sinus mode, the cup is rotated back and forth in sinusoidal fashion from -0.1309 to +0.1309 rad. This results in a shear, \( \gamma \), imparted to the test material (assuming no wall slip), oscillating from \( -\gamma_{\text{max}} \) to \( +\gamma_{\text{max}} \), where

\[
\gamma_{\text{max}} = \frac{r_0 + r_1}{2} \cdot \frac{0.1309}{r_0 + r_1}
\]

For both CS systems, the bulk material in the measuring gap is sheared from -1.505 to +1.505. Across the gap occupied by the surface film, the shear imposed will not be uniform (Williams and Williams, 1989), but using equation 5 as a guide, \( \gamma_{\text{max}} \) in the surface film oscillates very roughly from -0.077 to +0.077 in the short CS, and from -0.079 to +0.079 in the tall CS.

The rheometers were used mostly in Sinus mode. As well as a digital display proportional to \( \tau \), the instrument produces one analogue output (a voltage) proportional to \( \dot{\gamma} \) and another proportional to \( \gamma \). By connecting these two outputs to the x and y channels of a rapid-response, flat-bed graph plotter, a cyclic rheogram ("rheographe cyclique", Faure, 1989) was produced of \( \tau \) plotted against \( \gamma \).

![Figure 2](image)

Figure 2

Cyclic rheograms, taken from examples to illustrate: a) type 1, corresponding to Newtonian material; b) type 2, corresponding to linear viscoelastic behaviour, as in a Maxwell fluid (where the viscosity and elastic moduli of the material remain constant during deformation); c) type 3, similar to type 2, except that the plotter pen revolves anticlockwise (see text for explanation); d) type 4:1; pen describes curve showing components of rotation in both directions, in this case a figure-of-eight; e) type 4:2; pen describes a complex curve showing components of rotation in both directions. Vertical axis: \( \gamma \); horizontal axis: \( \dot{\gamma} \) (different scales). Letters A, B, C, D, E, F: (Fig. b) define line lengths in equations 6, 7 and 8. S, F: start, finish of a plot.

Rheographe cycliques (très exemplaires) pour en illustrer : a) type 1, comportement d'un matériau newtonien ; b) type 2, comportement viscoélastique linéaire, par exemple un fluide de Maxwell (où la viscosité et le module élastique restent constants durant la déformation) ; c) type 3, similaire au type 2, sauf que le stylo de la table traceuse tourne dans le sens contraire (voir le texte pour l'explication) ; d) type 4:1 ; le stylo trace une courbe avec des composants de rotation dans les deux sens, dans cet exemple comme un chiffre "8" ; e) type 4:2 ; le stylo trace une courbe complexe des composants de rotation dans les deux sens. Axe vertical : \( \gamma \); horizontal : \( \dot{\gamma} \) (échelles différentes). Les lettres A, B, C, D, E, F : (Fig. b) définissent les longueurs de ligne dans les équations 6, 7 et 8. S, F : début, fin d'une trace.
Rheograms produced by this system are shown in Figure 2a for a purely viscous liquid, and in Figure 2b for a material showing linear viscoelasticity (one in which \( \eta \) and \( G' \) remain constant during the measurement cycle). Other types of curves are produced by materials in which the viscous or elastic modulus changes during the measurement cycle. For a given CS geometry in which \( \gamma \) is forced to oscillate through a given amplitude and at a given angular frequency, \( \omega \), a calibration coefficient, \( c \), is provided. Then,

\[
\eta = c \sin \delta \cdot \text{length CB} \quad (6)
\]

\[
G' = c \cos \delta \cdot \text{length CB} \cdot \omega \quad (7)
\]

where \( \delta \) is the "loss angle", i.e., the phase difference between stress \( \tau \) and shear \( \gamma \) and the lengths refer to Figure 2b. The cyclic rheogram (Fig. 2b) is used to determine \( \delta \) as follows (manufacturers’ handbooks):

\[
\delta = \arccos \left( \frac{\text{length OA}}{\text{length OB}} \right) \quad (8)
\]

Williams and Williams (1989) reviewed further theoretical considerations for a variety of geometries and deformational regimes, albeit with much thicker suspensions and higher shear rates in mind.

**Rheometry: enhancement of precision**

The following precautions were taken to optimize data quality. To reduce air currents at both Grenoble and Bremerhaven, the CS was enclosed in a small Plexiglas box within a larger box protecting the whole rheometer. To reduce vibration, both rheometers were installed on massive microgram-balance-type tables. The Bremerhaven rheometer and its plotter were connected to a stabilized voltage supply, but this was not available at Grenoble, where step-like voltage changes in the mains supply affected the rheograms. Allowance was made for these step-like changes when measuring the rheograms. The plots were checked and recalibrated when necessary to allow for shrinkage and expansion of the plotting paper caused by humidity changes, and to allow for error due to the lines printed on the graph paper deviating up to 0.5° from the axes of the plotter. With these precautions, and by selecting appropriate expansion of the analogue outputs, a resolution was obtained of 10^-7 Pa under good conditions of vibration and voltage stability. At Grenoble the laboratory was temperature controlled (extreme limits about ± 0.5°C), and at Bremerhaven the temperature in the CS was maintained constant by a thermostated water jacket (also ± 0.5°C). Since the high-shear viscosity of seawater varies by about 3% per °C around the temperature of measurement (Miyake and Kozumi, 1948), and the values of \( \eta_{BE} \) of interest here, are obtained by subtracting \( \eta_{WS} \) from \( \eta \), better temperature control would probably have considerably improved the precision of measurement of \( \eta_{BE} \).

**Rheometry: calibration of rheometers**

No calibration material appears to be available for investigations at the low shear rates, \( \gamma \approx 2 \times 10^{-3} \) s^-1, and the low shear stresses, \( \tau \approx 2 \times 10^{-6} \) Pa, obtained in the present study. I attempted to use freshly double-distilled water as standard, but it generally developed apparent elasticity (probably due to a surface film; see below) within two to three hours, the time necessary to cool the sample to constant temperature and carry out a measurement at low \( \gamma \). Calibration using more viscous materials, such as some calibration oils or glycerol, would have given calibration measurements in which the interference due to surface effects would have been swamped out by components of \( \tau \) in the bulk material. I rejected the use of these materials for calibration, however, because the values of \( \tau \) measured for calibration would have been several orders of magnitude higher than those measured in the least viscous samples, and it is doubtful whether such a degree of extrapolation could be justified.

For the rheometer at Grenoble, it will be shown that application of the manufacturer’s calibration gave values for \( \eta_{WS} \) between 4.4 and 6.4% higher than the values given by Miyake and Kozumi (1948) in their Table 2 for \( \eta \) at high \( \gamma \), \( \eta_{MK} \) (users of this table should beware of some printing errors which become obvious on attempts at critical interpolation.) The manufacturers’ calibration has thus been used unchanged for the calculation of viscosity obtained with this instrument.

For the rheometer at Bremerhaven, the viscosity of the least thickened samples was found to vary similarly with shear rate but in a non-linear fashion. This has been interpreted as indicating different degrees of departure from the manufacturers’ calibration coefficient for different imposed shear rate, probably due to systematic error in the angular frequency, \( \omega \). Calibration was carried out post facto using the measurements made on four seawater samples of known salinity which had viscosity low relative to the other samples, and no detectable apparent elasticity. For calibration, it has been conservatively assumed that the mean of the measurements made on these samples corresponds to Newtonian behaviour. These low-viscosity samples included three from the North Sea survey, station

<table>
<thead>
<tr>
<th>Cruise</th>
<th>( r^2 )</th>
<th>( P )</th>
<th>( k )</th>
<th>( \eta_{WS} ) (mPa s)</th>
<th>( \eta_{MK} ) (mPa s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>July 1986</td>
<td>0.9990</td>
<td>1.46</td>
<td>0.00021</td>
<td>1.014</td>
<td>0.971</td>
</tr>
<tr>
<td>Nov. 1986</td>
<td>0.9993</td>
<td>1.36</td>
<td>0.00105</td>
<td>1.124</td>
<td>1.068</td>
</tr>
<tr>
<td>Mar. 1987</td>
<td>0.984</td>
<td>1.49</td>
<td>0.00042</td>
<td>1.080</td>
<td>1.015</td>
</tr>
<tr>
<td>May 1987</td>
<td>0.989</td>
<td>1.22</td>
<td>0.00020</td>
<td>1.073</td>
<td>1.073</td>
</tr>
<tr>
<td>North Sea</td>
<td>0.981</td>
<td>1.11</td>
<td>0.045</td>
<td>0.994</td>
<td>Note 1</td>
</tr>
</tbody>
</table>

Note 1: \( \eta_{MK} \) variable because of salinity differences. Values given in Appendix, Table 3.
1, 45 m, station 3, 30 m, and station 3, 41 m, and one sample taken from closed, 100 dm³ container in which seawater had been left to stand undisturbed in a constant-temperature (20°C) room for some days. The salinity of these four samples ranged only from 32.8 to 32.85.

Interpretation of the rheograms obtained

Cyclic rheograms of shear stress, τ, vs. shear rate, \( \dot{\gamma} \), could be divided into four types. Type 1, illustrated by Figure 2 a, corresponded to Newtonian behaviour, that is without any detectable effects of elasticity. Type 2 (Fig. 2 b), in which the plotter pen (indicating the \( \dot{\gamma} - \tau \) co-ordinate) revolved clockwise around a rough ellipse, corresponded to viscoelastic behaviour (behaviour due to both viscosity and elasticity). Type 3 rheograms (Fig. 2 c) were similar in form to type 2 rheograms, except that the pen rotated anticlockwise. In rheograms of type 4, the pen described curves showing both clockwise and anticlockwise components: the pen described either (1) "figures-of-eight" (Fig. 2 d) or (2) a curve in which the central part was described by rotation in one direction but loops at one or both extremes were described by rotation in the opposite direction (Fig. 2 e); occasional, even more complex rheograms involving components of rotation in both directions were also ascribed to type 4.

To separate surface-film from bulk-phase effects, most samples from the Mediterranean cruises in November, February, and May were measured using both a tall and a short CS. Where the central part of the rheogram showed a clockwise component (type 2 and in some of type 4), the measured storage modulus, \( G' \), was assigned a positive value. Where the central part of the rheogram showed an anticlockwise component, however, \( G' \) was assigned a negative value, and for rheograms of type 4 similar in form to figures-of-eight or other complex shapes, \( G' \) has been considered unquantifiable, and has been assigned a default value of zero.

It is frequently recommended that viscosity, \( \eta = G' / \dot{\gamma} \), be derived (manufacturers' instructions, see also Barnes et al., 1989) thus:

\[ \eta = \left( G''/G' \right)^{0.5} \dot{\gamma} \]

(9)

It will be shown in the Results section, however, that for curves to which \( G' \) was assigned a negative value (criteria given above) the following equation gave better experimental fit:

\[ \eta = \left( G''/G' \right)^{0.5} \dot{\gamma} \]

(10)

Equation 10 has thus been used to derive the results of \( \eta \) presented. The review of Williams and Williams (1989) concerns the problems of measuring cohesive, aggregative suspensions, but still at shear rates and stresses much higher than the lowest in the present study.

RESULTS

The complete data set for \( \eta \) and \( G' \) is presented for the Mediterranean and the North Sea in Appendix Tables 2 and 3 respectively.

Viscous components

To test the applicability of the present data of the model expressed by equations 5 and 6, the arithmetic mean of total viscosity \( \eta(\dot{\gamma}) \) was calculated for each shear rate and for each cruise. The value of \( \eta_w \) for each cruise was adjusted to obtain the highest correlation coefficient, \( r^2 \), of \( \log_{10} (\eta(\dot{\gamma}) - \eta_w) \) vs. \( \log_{10} (\dot{\gamma}) \). Table 2 shows the values found for \( r^2 \), \( k \), and \( \eta_w \). For comparison, the viscosity values, \( \eta_{HM} \), proposed by Miyake and Koizumi (1948) for corresponding values of salinity and measurement temperature are also given, as well as values of the ratio \( \eta_w / \eta_{HM} \). Figure 3 shows the relationship between \( \eta_w(\dot{\gamma}) \) and \( \dot{\gamma} \). The use of arithmetic means of \( \eta_w \) from a skewed distribution to present overall parameters gives relatively more weighting to viscometric properties in the more viscous samples. These are the samples measured the most precisely. The high resultant values of \( r^2 \) support the Ostwald power-law model (equation 6) as a good approximation to the mean viscometric behaviour of the non-Newtonian component in our samples. As shown in Table 2, for all the data from each cruise, \( P \) was 1.1 for the North Sea samples and varied from 1.22 to 1.49 for the different Mediterranean cruises. The Mediterranean data represented in Figure 3 were previously published in Jenkinson (1989, Fig. 1 b) in preliminary form (calculated using equation 9).

Standard deviation in excess viscosity

Figure 4 shows that as \( \dot{\gamma} \) was increased, not only did the standard deviation of the viscosity, SD [\( \eta(\dot{\gamma}) \)] strongly decrease,
Appendix Table 2

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Measured viscosity (mPa s) | Measured elastic modulus (mPa)

\[ \frac{\eta_E(\gamma)}{\eta_H(\gamma)} \]

but so did the ratio \( \frac{\eta_E(\gamma)}{\eta_H(\gamma)} \). This reflects the decreasing importance of \( \eta_E(\gamma) \) (which is intrinsically variable) relative to \( \eta_H \) (which is intrinsically stable) as \( \gamma \) increases.

To investigate the variation of \( \eta_E \) over different values of \( \eta_H \) and \( \gamma \), the SD(\( \eta_E(\gamma) \)) has been plotted against \( \eta_H(\gamma) \) (Fig. 5). The curve "hugs" the upper side of a straight line representing SD(\( \eta_E(\gamma) \)) = \( \eta_H(\gamma) \) with ratios of SD(\( \eta_E(\gamma) \))/\( \eta_H(\gamma) \) mostly between 1 and 3, irrespective of \( \gamma \), except at values of \( \eta_H(\gamma) \) below 100 mPa s. Below this excess viscosity, the curve "peels away" from the straight line, SD(\( \eta_E(\gamma) \)) = \( \eta_H(\gamma) \), to give higher values of SD(\( \eta_E(\gamma) \))/\( \eta_H(\gamma) \), the highest recorded being 13 at \( \eta_H(\gamma) = 1.3 \) mPa s. This represents a higher relative importance of errors in \( \eta \) when \( \eta \) is low. Possible sources of these errors may include: 1) imprecision in the instrument, in the plotter and in measurements made of the plotted output, 2) in Mediterranean samples only, variation in salinity acting on
La viscoélasticité de l'eau de mer.

Vitesse et module de conservation mesurés à des vitesses de cisaillement entre 0,0021 et 0,975 s⁻¹ dans les échantillons d'eau de mer de la Mer du Nord.

In Figure 6 measured elastic modulus G' is plotted against measured excess viscous modulus, G'' = nE⁻¹, for all measurements where G' = 0. There is considerable clustering of points around the origin, and there were 107 cases where G' was negative and 61 where it was positive (plus 71

Elastic components in the Mediterranean samples

Moyenne, écart-type (SD) et 2 x écart-type de la moyenne (SE) (limite de confiance 95 % approximativement) pour la viscosité (η) ainsi que SD(η)/moyenne(η) pour chaque vitesse de cisaillement et pour chaque sortie. Noter que l’échelle verticale est la même pour les données de la Mer du Nord et l’eau de mer méditerranéenne.

Mean, standard deviation (SD) and 2 x standard error (SE) (approximately 95% confidence limit) for viscosity (η) as well as SD(η)/mean(η) for each shear rate and cruise. Note that the vertical scale is the same for the data from the North Sea and Mediterranean.
cases where $G'$ was classed as zero). For the set of data points in which $G' = 0$, the largest absolute values of the measured elastic modulus, $G''$, however, were represented positive $G'$. In order to compare independent data points, $G''$ has been compared with $G''_E$ (where the overbar signifies the mean of all measurements for each sample) in which $G' = 0$. While there was no correlation discernible between $G''$ and $G''_E$, correlation was significant between $G''$ and $G''_E$ ($r^2 = 0.00006, 0.00001 < P < 0.0001$ (distribution not illustrated)). Furthermore, if (for reasons explained in the following section) $G''$ is multiplied by 2.24 for sets measured using the tall CS, the closeness of the relationship is improved ($r^2 = 0.36, 0.00001 < P < 0.00005$).

Tests of whether surface-film or bulk-phase effects were responsible for the measured rheological properties

Because the area of the side of the bob bordering the measuring gap (the surface on which measured bulk-phase forces act) is greater in the tall CS than in the short one, while other dimensions (particularly the width of the measuring gap and the diameters of both the bob and of the bob stem) are identical (Fig. 1 a, b), the manufacturer's calibration sheets indicate that a given tangential force exerted by the surface film on the bob stem, producing the same torque in both CS systems, is equivalent to a bulk-phase shear stress, $\tau$, 2.24 times greater in the small CS than in the tall one. Where $\text{comp}(S)$ and $\text{comp}(T)$ are, respectively, the mean of any rheological component measured in the small CS and the tall CS (and calculated from calibration coefficients for bulk-phase components), a rheological component due exclusively to bulk-phase effects should give $\text{comp}(S)/\text{comp}(T) = 1$, while one due exclusively to surface-film effects should give $\text{comp}(S)/\text{comp}(T) = 2.24$.

Figure 7 shows the excess viscous modulus measured in the tall CS, $G''_E(T)$, plotted against that for the same sample measured in the small CS, $G''_E(S)$. An obvious absence of correlation is indicated between $G''_E(T)$ and $G''_E(S)$. To carry out statistical analysis on independent variables, $G''_E(T)$ was plotted against $G''_E(S)$ (Fig. 8). The overall mean of $G''_E(T)$ 3.2 $\mu$Pa (SD 9.1) was not significantly different from that of $G''_E(S)$ 5.0 $\mu$Pa (SD 7.0), as determined by Student's paired t-test ($n = 23$). It is thus concluded that the relationship is statistically compatible with the hypothesis that all the excess viscosity was contributed by bulk-phase effects.

By contrast, the same overall mean of $G''_E(T)$, 3.2 $\mu$Pa (SD 9.1) is significantly smaller than that of the overall mean of $G''_E(S)$, 2.24, 11 $\mu$Pa (SD 16) ($0.01 < P < 0.05; n = 23$). It is thus concluded that this relationship is not compatible with a hypothesis that all the excess viscosity was contributed by the surface film. There was no significant correlation or slope in either of the above graphs, indicating no significant relationship between excess viscosity in pairs of measurements (using the tall CS and the small CS) made on the same sample. The intercept, 4.6 $\mu$Pa ($95\%$ confidence limit $\pm 3.8$) was significantly $> 0$, simply reflecting that the overall mean of $G''_E(T)$ is significantly $> 0$.

Proceeding similarly for the measured elastic modulus, Figure 9a shows $G'(T)$ plotted against $G'(S)$. There is no significant correlation or slope. The overall mean of...
G'(T) - 3.1 μPa (SD 7.4) is (of opposite sign but) only marginally significantly different from that of G'(S), +4.4 μPa (SD 25.4) (0.05 < P < 0.1; n = 46), while SD[G'(T)] is less than SD[G'(S)] by a factor of 3.4. Plotting G'(T) vs G'(S) (Fig. 9b), the overall means are now significantly different (0.01 < P < 0.05; n = 46).

Figure 10a shows |G'(T)| plotted against |G'(S)|. Again there is no significant correlation or slope. The overall mean of |G'(T)|, 5.3 μPa (SD 6.0), is significantly less than that of |G'(S)|, 16 μPa (SD 20), (0.0005 < P < 0.0001; n = 46) by a factor of 3.04. This result is not compatible statistically with a hypothesis that all the measured positive and negative elasticity could have been contributed by the bulk phase. Figure 10b shows (|G'(T)| x 2.24) plotted against |G'(S)|. The overall mean of (|G'(T)| x 2.24) 11.8 μPa (SD 13.5), is still less than that of |G'(S)| (unchanged), now by a factor of 1.36, but the difference is not significant. This result is compatible statistically with the hypothesis that all the measured positive and negative elasticity was contributed by the surface film. As with the excess viscous modulus, G''(S), no significant correlation was found between duplicate measurements (tall and small CS) of the same samples, in either G' or G''.

From these statistical considerations alone, it can be deduced that: 1) surface film effects were responsible for much or all of the measured elasticity; 2) surface film effects were responsible for none or some of the measured excess viscosity, but not all of it; 3) bulk phase effects were responsible for none or some of the measured elasticity, but not all of it; 4) bulk phase effects were responsible for some or all of the measured excess viscosity.

The absence of any discernible correlation between duplicate measurements (tall and small CS) of either viscosity or elasticity suggests that measured rheological variation within the Mediterranean cruises was dominated by within-sample heterogeneity.

**Investigation of surface effects with a surface CS**

Surface effects were measured at Bremerhaven using a surface bob (Fig. 1c). Figure 11 shows the results obtained for the surface film of deionized double distilled water (DDDW) which had been kept in a laboratory wash bottle for several days. The surface shear stress, τ_{surf}, oscillated with the same frequency as that of cup rotation and with a half amplitude = 0.03 mN m\(^{-1}\) (Fig. 11). The mean value and the amplitude of τ_{surf} were both practically independent of cup rotation speed and hence of surface shear rate \(\dot{\gamma}_{surf}\). Oscillation was quasi-sinusoidal except for some pre-peak instability (arrowed in Fig. 11), indicating yielding in the film or slipping at its edge.

With filtered Skeletomella culture, quasi-sinusoidal oscillation in τ_{surf} also occurred, but no instability was discernible. On standing of this culture in the CS (between measurements), the amplitude of oscillation in τ_{surf} showed a quasi-exponential increase with time. This increase may reflect adsorption of bulk-phase polymers on to the surface, and perhaps also chemical or microbiological network formation.
Oscillation did not occur when the procedure was carried out with any CS system when it was empty, indicating that magnetism in the CS was not responsible.

Whatever the mechanism responsible for the oscillation in $\theta_{surf}$ (this is treated further in the "Discussion"), it is likely that tangential forces of a similar type acted also on the stems of the bobs used in sinus mode for the bulk-phase measurements (the tall CS and the short CS).

Assuming that shear is uniform across the surface from the wall of the CS cup to the edge of the surface-phase bob and neglecting any effects produced by the meniscus or by variations in the amount the short CS was filled on the wall-to-bob distance, shear rate in the measuring gap. In practice, values are likely to be higher near the bob stem (Barnes et al., 1989).

If the imposed shear, $\gamma$, was oscillated sinusoidally over a part of the curve of torque vs. rotation with positive slope (illustrated in Fig. 12 by Bar D), then even in the absence of bulk-phase elasticity, a trace of $\tau$ vs. $\gamma$ would rotate clockwise (Inset D), giving a positive value for measured apparent elasticity. If, however, $\gamma$ was oscillated over a part of the curve with negative slope (Bar C, Inset C), the trace would rotate anticlockwise, giving negative apparent elasticity. If $\gamma$ was oscillated over a part showing a maximum or a minimum (Bars A,B; Insets A,B) the curves illustrated would result. Traces resembling figures-of-eight are likely to result where the change in direction of rotation affected the curve of $\tau$ in relation to CS position (both clockwise and anticlockwise). The largest amplitudes of torque encountered represented tangential forces of 0.17 mN m$^{-1}$ (distilled water), 0.034 mN m$^{-1}$ (0.2 µm filtered sea water) and 2.0 mN m$^{-1}$ (filtered Skeletonema culture). Measurements carried out using the surface bob in sinus mode using both the filtered sea water and the filtered Skeletonema culture, gave curves characteristic of positive or negative elasticity but without viscosity.

**Elastic components in the North Sea samples**

The measured values of $G'$ (Appendix Tab. 3) are plotted against $G''_0$ in Figure 15. Those values of $G'$ obtained by...
0.973 s⁻¹ are thought to be contaminated by interaction among rheological properties, inertial effects in both the bob and the test material, and finite reaction time of the torque-plotting system. The viscosity values (obtained by correction using the possibly erroneous values of G') seem reasonable, however.

Excluding data obtained at $\dot{\gamma} = 0.973$ s⁻¹, no North Sea sample showed negative measured G', while 35 positive values were obtained, suggesting that the mechanisms contributing to measured G' in the North Sea samples were different from those in the Mediterranean water. That the North Sea data were all obtained with the same CS geometry has precluded statistical tests similar to those carried out on the Mediterranean water, to determine whether surface or bulk effects were responsible.

Comparison of Figure 13 with Figure 6 shows that some of the values of both G"E and G' (maxima 700 and 600 μPa respectively) were an order of magnitude higher than the highest found in the Mediterranean samples (corresponding maxima 40 and 80 μPa). Figure 13 shows the positive relationship between G"E and G'. This relationship is contributed only by the higher values, the cluster of points near the origin (Fig. 13 inset) showing no such strong relationship.

Rank-value distributions of measured rheological properties

The Zipf-Mandelbrot log(rank)-log(frequency) distribution is frequently used to illustrate the distribution of organisms among the different taxa in an assemblage (or in a sample) (Frontier and Pichol-Viau, 1991). The rank of the most abundant taxon is scaled as unity. We have adapted this type of plot to illustrate the distribution of parameter values in any set of them. Sets with different numbers of values are rendered comparable by dividing rank by the number of data points in the set, giving a plot of log(rank/n) vs. log(paramete value). Using this plot for values of measured G"E and G', negative measured values (as log(-value)) are shown separately, but n is the total number of samples (negative, zero and positive) in the set. In both the rank-frequency plot and the rank-value plot the slope of the graph represents the Gaussian standard deviation, SDG. How SDG varies with rank is thus obvious from the plot.

The two variables presented are G"E (Fig. 14a) and G' (Fig. 14b), where the overbar signifies the arithmetic mean in measurements of a sample at all values of $\dot{\gamma}$ (in these cases, excluding $\dot{\gamma} = 0.973$ s⁻¹). Series of measurements carried out in the tall CS and the short CS (Mediterranean study) are treated as separate samples since they showed no correlation, as are measurements on duplicate samples (some North Sea samples).

Three out of the four Mediterranean samples with the highest mean excess viscous modulus, G"E, were also among the four samples with the highest values of the mean elastic modulus, G'. Similarly, six of the seven North Sea samples with the highest values of G"E were among the seven with the highest values of G'; and their respective rank orders were almost the same (Fig. 14a, b). In the seven North Sea samples with the highest values of G"E and G', the ratio G'/G"E varied only from 0.23 to 0.72, indicating that similar polymers may have caused most of the viscous and elastic thickening. That values of G' in the Mediterranean are in the majority negative suggests that a systematic negative error was introduced by the measurement technique, perhaps due to a lag in stress output relative to that of the CS position output in the rheometer-recorder system. That negative values of G' occurred only at $\dot{\gamma} = 0.973$ s⁻¹ in measurements of the North Sea samples (despite likely positive and negative surface-film errors) supports this suggestion. The four largest absolute values of G' measured in the Mediterranean samples were all positive, however, suggesting that bulk-phase elasticity was dominating both that due to surface effects and that due to systematic measurement error in measured values of G' in these samples. The ratios of G'/G"E ranged from 0.22 to 11.2 in these samples suggesting that the material contributing to the bulk-phase rheological properties in the Mediterranean samples was structurally more diverse than that in the North Sea samples. That excess viscosity in the North Sea samples was closely correlated with chlorophyll content mostly due to Phaeocystis blooms (Jenkinson and Biddanda, in preparation) suggests that this material comprised mainly exopolymers derived from a single species.

The rank-value diagram of G"E (Fig. 14a) resembles a straight line of slope -0.9 from ranks 1 (+43 μPa) to 33 (+1.6 μPa) for the Mediterranean samples, while for the North Sea data set the curve approximates also to a straight line, but less closely, from ranks 1 (+540 μPa) to 9 or 10 (±2 μPa), with a slope of -2.6. At higher values of scaled rank, the slope increases rapidly for both
Figure 14

Zipf-type graphs of elastic and excess viscous moduli vs. (sample rank/total number of samples). Duplicate subsamples are treated as separate samples. Logs of both positive and negative measured values are plotted, using different symbols, and values of zero are indicated separately. The scale of the horizontal axis is twice that of the vertical one. a) mean (over all shear rates for each sample) excess viscous modulus, $G^>^E$: b) mean elastic modulus, $G^E$ (any values measured at $\dot{\gamma} = 0.973$ s$^{-1}$ excluded from mean).

Courbes de type Zipf du module élastique et du module visqueux excédentaire vs. (rang de chaque échantillon/nombre d’échantillons). Des mesures de sous-échantillons sont comptées comme d’échantillons à part entière. Les logarithmes des valeurs positives, zéro et négatives sont indiqués avec des symboles différents. L’axe horizontal est d’une échelle deux fois inférieure à l’axe horizontal. a) moyenne (des mesures à toutes les vitesses de cisaillement pour chaque échantillon) du module de viscosité excédentaire, $G^>^E$: b) moyenne du module élastique, $G^E$ (toute mesure faite à $\dot{\gamma} = 0.973$ s$^{-1}$ est exclue de la moyenne).

Mediterranean and North Sea data sets. In the corresponding parts of the curves where $G^E$ was negative (and where log(-$G^E$) was plotted against scaled rank), no straight line section appears with decreasing rank, the curves for both sea areas remaining rather concave. The highest negative value of $G^E$ recorded were rather similar, - 6.3 μPa (Mediterranean) and - 3.3 μPa (North Sea). The positive near-zero parts and the negative parts of the curves for the two data sets resemble each other in both value and slope, indicating similar means and SD_{G}. At high positive values, however, both value and slope are markedly different. This is interpreted as indicating similar means and SD_{G} for each of the two data sets for those parts of the data dominated by measurement artefacts, but very different values and variance for the parts dominated by environmental properties.

It is concluded that at values of $G^E$ high enough for the environmental component to be separated from measurement artefacts (~ 2 μPa), the North Sea samples possessed higher mean and SD_{G} in excess viscosity than the Mediterranean samples. Part of this extra variability may have derived from the sampling strategy, which targeted five hydrological layers in the North Sea, including the air-sea and the sea-sediment interfaces, while the Mediterranean study involved mainly mid-water layers. Although no biological measurements exist for our Mediterranean data set, further variability in the North Sea samples as well as their higher mean values may have resulted from higher abundance and patchiness in polymer content associated with the abundant and patchy distribution of phytoplankton.

DISCUSSION

Bulk-phase rheological properties of the samples

At $\dot{\gamma} = 0.0021$ s$^{-1}$, the measured viscosity of the meso-oligotrophic Mediterranean seawater samples was 0.71 to 19 times that of the solution viscosity $\eta_w$, which is due to water and salts alone. The corresponding values for $\dot{\gamma} = 0.286$ s$^{-1}$ were 0.92 to 1.12.

At $\dot{\gamma} = 0.0021$ s$^{-1}$ the viscosity of samples taken from the North Sea, where patchy blooms of Noctiluca scintillans and Phaeocystis sp. were taking place was 0.99 to 127 times $\eta_w$. Viscosity at $\dot{\gamma} = 0.286$ s$^{-1}$ was 0.96 to 3.2, and at $\dot{\gamma} = 0.973$ s$^{-1}$ it was 0.98 to 1.21 times $\eta_w$.

That values of SD [η_{E}(\dot{\gamma})]/η_{E}(\dot{\gamma}) or each cruise and shear rate (except at the lowest value of η_{E}(\dot{\gamma}), where measure-
ment error is believed to have been dominant), varied from about 1 to about 3 indicates a very high rheological patchiness or "lumpiness". Despite the vigorous mixing associated with sampling, this lumpiness was present within the samples from which duplicate 0.5 to 1.0 cm³ subsamples were measured. This suggests that centimetre-scale (or smaller) flocculation occurred in the samples during storage and transport (less than about one day). Flocculation is important in marine colloids (Morel and Gschwend, 1987), and cm-scale variation in fluorescence in situ may reflect similar variation in polymer concentration and viscosity (Carlson, 1991). The observation of exceptional thickening in some plankton blooms (see "Introduction"), the correlation between η and chlorophyll concentration in the present North Sea study (Jenkinson and Biddanda, in preparation), and the increased bulk-phase viscosity found in some surface slicks (Carlson, 1987) indicates that seawater thickening varies also at larger scales.

Carlson et al. (1987) suggested that artificially high values of viscosity might be produced in CS rheometry due to colloidal material being scavenged from the bulk phase on to the surfaces of the CS. That surface effects in the CS were found to increase frequently over time suggests that organics are scavenged by the air-seawater interface. Any scavenging on to either the air-liquid surface or the metal-liquid surface would take polymers out of the bulk phase, and would tend to reduce bulk-phase thickening. Adsorption on to the cleaned glass walls of the sampling bottles might have further reduced measured values of thickening.

Generally, in gels P ≥ 1, but in polymers without crosslinks, P < 1 and a Newtonian plateau in η (P = 0) occurs over a range of γ (Morris, 1984). The consistently high values of P found over two or more orders of magnitude in γ in the present study, thus suggest that the non-Newtonian behaviour was contributed largely by highly cross-linked gel. Material secreted into culture by green and red algae, was shown by its turbulent-drag reducing properties to consist of very complex, polymeric, aggregative gels (Ramus and Kenney, 1989; Ramus et al., 1989). In contrast, the viscosity of a culture of Amphidinium sp. over a range of γ from 0.017 to 129 s⁻¹ showed a low-γ Newtonian plateau (P = 0), and a higher range of γ in which P = 0.5 (Jenkinson, 1986), indicating that thickening was due principally to overlapping polymer molecules (Morris, 1984; Barnes et al., 1989). Similarly, in cultures of Dunaliella marina and of Noctiluca scintillans together with D. marina (Jenkinson, 1986), as well as in a culture of Gyrodinium cf. aureolium and in water filtered from a suspension of N. scintillans (Jenkinson, 1993), no low-γ plateaux occurred, values of P were lower than in the present work, and inflexions, including steps, occurred in the slope. This suggests that both cross-linking and overlapping of the polymers were responsible for the rheological properties to different relative extents at different shear rates.

A ratio around unity (0.22 to 11) is indicated for G'/G'' in the bulk-phase polymeric material in the present study. Corresponding to their lower values of P, values obtained for G'/G'' were also generally lower in phytoplankton suspensions, further suggesting a less cross-linked polymer structure. Values for G'/G'' were: 0.4 in the mixed culture of Noctiluca scintillans and Dunaliella marina (calculated from data presented by Jenkinson, 1986); 0.2 to 0.9 in the culture of Gyrodinium cf. aureolium, mentioned above; 0.2 to 0.3 in water filtered from a suspension of N. scintillans (Jenkinson, 1993). Similarly Frew and Nelson (1992) found that the ratios of both (surface-film compression elastic modulus)/(film pressure) and carbon/nitrogen were higher in samples from an area relatively low in biological activity, suggesting that the film material had, in ageing, become more cross-linked.

Silicate and organic C are present in seawater in comparable amounts, ~ 0.2 and ~ 0.1 mM respectively, and both form polymeric complexes, although silicate begins to polymerise at concentrations ≥ 1.5 mM (Stumm and Morgan, 1981). Dissolved silicate strengthens some organic polymers by cross-linking and is surface active (Schwarz, 1973; Grant and Long, 1985; Jarvie, 1986; Zhang et al., 1991). Silicic acid thus enhances seawater rheological properties by adsorbing on to surfaces provided by colloidal organic polymers (Morel and Gschwend, 1987). The idea is somewhat supported by Holibaugh et al.'s (1991) finding that "dissolved" silicate is occasionally retained by ultrafiltration.

Possible origin of surface-film shear forces

When shear forces in the surface film were measured in continuous rotation of the CS, the regular, and frequently approximately sinusoidal, oscillation of these forces with the same period as that of CS rotation indicates a large degree of spatial integrity in the surface film during rotation. Exactly how this integrity was maintained remains unknown, although interaction of two plaques, one adhering to the bob and the other to the wall of the cup, seems likely (Lavén, personal communication).

Measurements made with both continuous rotation and sinusoidal oscillation, as well as with both the surface-phase bob and with the bulk-phase bobs, gave the following maximum shear strengths: 2 mN m⁻¹ for Skeletonema culture; 0.17 for aged distilled water; 0.03 for 0.2-μm filtered seawater; 0.03 mN m⁻¹ for unfiltered or filtered (0.5 mm) seawater samples. The relatively high value for the Skeletonema culture suggests that diatoms and their setae might have reinforced the material habitually in the surface film, a mechanism suggested by Wyatt et al. (1993) for the bulk phase. No previous data on shear properties appear to exist for the seawater surface film. For film pressure (i.e. compression strength), however, Van Vleet and Williams (1983) found values in sea-surface films of 1.5 to 15 mN m⁻¹, about two orders of magnitude higher than the maximum shear forces we measured in the surface film of seawater. Ting et al. (1984), working with surface films of octanionic acid, also found film pressure to be about two orders of magnitude higher than shear strength, so shear strength and film pressure in sea-surface films may each be produced by the same material. Barger and Means (1985), who also measured film pressures, concluded that surface films are composed of material similar to very large poly-
Might organic matter contribute to the high-shear component of $\eta_w$?

To estimate the role of salinity in determining seawater viscosity, Miyake and Koizumi (1948) measured high-$\gamma$ viscosity in increasingly diluted seawater. Assuming that they used pure water as diluant, they diluted the non-conservative organic matter along with the conservative salt. Interference by surfactants or sticky material may furthermore be suspected from Miyake and Koizumi's observation that, "The most important source of error might be due to a delicate change in the condition of the inner wall of the capillary, but it was impossible to estimate its exact magnitude". Some organic matter might contribute to $\eta_w$. To separate $\eta_w$ from $\eta_E$ in future studies, it will be necessary to make high-$\gamma$ measurements on waters of different original salinity.

That, in the present study, some values of $\eta_E$ have been calculated as negative could reflect (in addition to experimental errors) a non-conservative polymeric component contributing to high-$\gamma$ viscosity.

Importance of viscoelastic thickening to turbulence and mixing

A simple model was proposed by Jenkinson (1986) to predict the effect of homogeneous excess viscosity (as $K$ and $P$) on Kolmogorovian (non-intermittent) turbulence. If the mean values of $\gamma$-dependent $\eta(\gamma)$ found on the five cruises of the present study (Tab. 2) are used in this model, the changes indicated in Figure 15 are obtained. The aim of this model is to provide only a quantitatively reasoned guess about modification of turbulence by polymeric thickening. Serious prediction must await better information about both rheological parameters and marine turbulence. Relevant rheological parameters for gels include: elastic modulus; yield stress; yield point; the same parameters for both shearing and extensional (also called elongational) flow; time dependence of all these parameters. The variation of all these parameters with length scale, together with lump shape, are also critical. Because turbulence is always intermittent and $P$ is high, the excess viscosity increases intermittently by reducing deformation rates proportionately more when they are already low. For a given overall intensity of turbulence (rms $\gamma$) when other things are equal, mixing parameters should in addition be negatively related both to $G'$ and to the Trouton ratio (elongational viscosity/shear viscosity) (Barnes et al., 1989). Furthermore, lumpiness (i.e. $SD_P$) in each of these parameters should contribute to increased intermittence and reduced mixing. Wyatt et al. (1993) have suggested how viscosity and structure may be contributed to bulk-phase seawater, otherwise than by polymers.

CONCLUSIONS

The viscosity of bulk seawater is composed of a Newtonian viscosity $\eta_w$, due to water and salt and independent of shear rate, on which is imposed an excess viscosity $\eta_E$ related to shear rate by an inverse power law. Total viscosity,$$
\eta = \eta_w + \eta_E, \text{ where } \eta_E = k_1 \gamma^{-p}
$$
Since $P$ was found to exceed 1, the seawater possesses a yield stress, which is a shear stress ($\eta(\gamma)$) below which the sea water gels. Strongly covarying with $\eta_E$ is a measurable elastic modulus $G'$. Both $\eta_E$ and $G'$ are distributed in a lumpy (rheologically heterogeneous) fashion, and are due to

\begin{figure}
\centering
\includegraphics[width=\textwidth]{figure15}
\caption{Effect of measured and observed thickening on the Kolmogorov length-scale, calculated from my previous model (Jenkinson, 1986). Actual turbulent length scale is around forty times that of the Kolmogorov scale (Jenkinson, 1986; Lazier and Mann, 1988; Yamasaki et al., 1991). The curves represent the arithmetic mean viscometric properties [relation of $\eta(\gamma)$ to $\gamma$], for each Mediterranean and North Sea cruise. For comparison, curves for Newtonian (unthickened) water and for Gyrodinium cf. aureolum-bloom water observed to trap 0.1 to 0.5 mm diameter bubbles (assuming that $P = 1$) are also shown. Effects of elasticity, lumpiness, time dependence, elongational viscosity, etc. are not taken into account.}
\end{figure}

L'effet des épaissements mesurés et observés sur l'échelle de longueur de Kolmogorov, estimé à partir de mon modèle antérieur (Jenkinson, 1986). La vraie échelle de longueur turbulente est environ quarante fois plus importante (Jenkinson, 1986; Lazier et Mann, 1988; Yamasaki et al., 1991). Les courbes représentent les moyennes arithmétiques des propriétés viscométriques [relation entre $\eta(\gamma)$ et $\gamma$] pour chaque sortie en Méditerranée et pour la croisière en Mer du Nord. Pour comparaison, les courbes correspondantes sont données pour l'eau newtonienne (non-épaisse), ainsi que pour l'eau dans une floraison de Gyrodinium cf. aureolum, où a été observée la rétention de bulles de diamètre compris entre 0.1 et 0.5 mm (il est supposé ici que $P = 1$). Les effets, entre autres, de l'elasticité, de la flocculation en grumeaux, de la dépendance du temps et de la viscosité élongationnelle ne sont pas pris en compte.
viscoelasticity of seawater

principally to organic polymers with a flocculent tendency, produced largely by phytoplankton. These polymers appear similar to, and exchange with, those responsible for viscosity and elasticity in the sea-surface film. A model of turbulent length scale in relation to η, predicts that turbulence is damped the most, in relative terms, both in zones already low in turbulence and in those of high biopolymer content. The high value of P and the lumpy distributions of both η and G' all make turbulence more intermittent. In much of the sea, flow and mixing, particularly at small scales (< 100 Kolmogorov length), are under strong biological influence.

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Fig. 10a shows $\bar{G}'(T)$ plotted against $\bar{G}'(S)$. Again there is no significant correlation or slope. The overall mean of $\bar{G}'(T)$, 5.3 μPa (SD 6.0), is significantly less than that of $\bar{G}'(S)$, 16 μPa (SD 20), (0.0005<$P<$0.0001; n = 46) by a factor of 3.04. This result is not compatible statistically with a hypothesis that all the measured positive and negative elasticity could have been contributed by the bulk phase. Fig. 10b shows $(\bar{G}'(T) \times 2.24)$ plotted against $\bar{G}'(S)$. The overall mean of $(\bar{G}'(T) \times 2.24)$, 11.8 μPa (SD 13.5) is still less than that of $\bar{G}'(S)$ (unchanged), now by a factor of 1.36, but the difference is not significant. This result is compatible statistically with the hypothesis that all the measured positive and negative elasticity was contributed by the surface film. As with the excess viscous modulus, $G''_e$, no significant correlation was found between duplicate measurements (tall and small CS) of the same samples, in either $G'$ or $|G'|$. 